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## Algorithmics

## Undergraduate $2^{\text {nd }}$ year (S4) - API <br> Final Exam \#4 (P4) <br> 16 May 2017-10h <br> Answer Sheets

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Answers 1 (MST and SP ... - 3 points)

1. The directed graphs on which the Bellman algorithm can be executed are:
2. The algorithm determining the mst of an undirected graph whose principle is close to that of Dijkstra is:
3. Highlight the connections you select to represent an mst of the graph.

4. Highlight the connections you select to represent the shortest path tree from the "power plant" vertex.


Answers 2 (Condensation - 4 points)

## Specifications:

The function condensation $(G, s c c)$ builds the condensation $G_{R}$ of a digraph $G$, with $s c c$ its component list. The function returns $G_{r}$ and the vector of components: a vector that give for each vertex, the number of its component (the vertex in $G_{R}$ ).

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Answers 3 (Digraphs and Mystery - 3 points)
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|  | Call number | Returned result |
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| (a) test $\left(G_{2}\right)$ |  |  |
| (b) test $\left(G_{3}\right)$ |  |  |

2. What is the information returned by test ( $G$ )?

## Answers 4 (T-spanner - 10 points)

1. (a) $t$-spanners for a stretch factor of 2
(2) (5)
(1) (4)
(7)
(0) (3) 6
(b) $t$-spanners for a stretch factor of 5
(2) (5) 8
(1) (4) 7
(0) (3) 6
2. (a) Specifications:

The function Dijkstra(G, src, dst) returns the length of the shortest path between $s r c$ and $d s t$ in $G,+\infty$ if there is no path.

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(b) Specifications:

The function pathGreedy $(n, L, t)$ returns a $t$-spanner (with stretch factor $=t$ ) for the set of $n$ points (number form 0 to $n-1$ ) with $L$ the list of triplets ( $\mathrm{p}, \mathrm{q},|p q|$ ) (as described above).

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bonus When the stretch factor is $n-1$ with $n$ the number of points, what is the $t$-spanner?

