

**ALGO  
MCQ**

**1. In a 2.3.4 tree, a k-Node does have ?**

- (a) k-1 children
- (b) k-1 elements
- (c) k children
- (d) k elements

**2. In a 2.3.4 tree, the minimum value is ?**

- (a) the first key of the root of the tree
- (b) the last key of the right-most leaf of the tree
- (c) the first key of the left-most leaf of the tree
- (d) the last key of the left-most leaf of the tree
- (e) the first key of the right-most leaf of the tree

**3. A 2.3.4 tree is ?**

- (a) a search tree
- (b) a binary search tree
- (c) an A-V.L.

**4. A left-left rotation is a \_\_\_\_\_ rotation?**

- (a) single
- (b) double
- (c) triple
- (d) that does not exist

**5. When using the insertion of an element in an A-V.L. tree, the resulting tree is systematically unbalanced?**

- (a) Yes
- (b) No
- (c) It depends

**6. The complexity of the positive search, for an element in a BST, ending on a node v is?**

- (a)  $2 * \text{depth}(v) + 1$
- (b)  $2 * \text{depth}(v) + 2$
- (c)  $\text{depth}(v) + 1$
- (d)  $\text{depth}(v) + 2$
- (e) None of the four previous answers

7. The properties of a 2.3.4 tree are ?

- (a) a B-tree of order 4
- (b) all its leaves are at the same depth
- (c) the keys are in decreasing order in the same node
- (d) for each key x, the keys of the right subtree are strictly greater than x
- (e) for each key x, the keys of the left subtree are strictly less than x

8. A binary search tree  $T = \langle r, L, R \rangle$  H-balanced is a tree ?

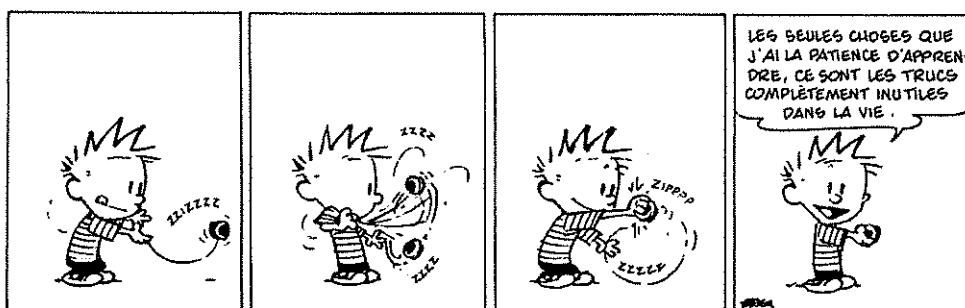
- (a) labeled
- (b) fitted with an order relation
- (c) such that at any node  $h(G) - h(D) \in [-1, 1]$

9. the transformation of the tree  $\langle a, \emptyset, \langle b, \emptyset, \emptyset \rangle \rangle$  to the tree  $\langle b, \langle a, \emptyset, \emptyset \rangle, \emptyset \rangle$ , where the letters are the nodes and  $\emptyset = \text{arbrevide}$ , is done using ?

- (a) a left rotation
- (b) a right rotation
- (c) a left-right rotation
- (d) a right-left rotation

10. A balanced search tree is always binary?

- (a) true
- (b) false



# MCQ 8

Monday, 20 May

## Question 11

Let  $A = \begin{pmatrix} 1 & -1 \\ -3 & 2 \end{pmatrix}$ ,  $B = \begin{pmatrix} -4 & -1 \\ 0 & -3 \end{pmatrix}$  and  $C = \begin{pmatrix} 1 & -1 & 0 \\ -3 & -2 & 5 \end{pmatrix}$ .

- a.  $A + B$  exists and its value is  $A + B = \begin{pmatrix} -3 & -2 \\ -3 & -1 \end{pmatrix}$
- b.  $A + C$  exists and its value is  $A + C = \begin{pmatrix} 2 & -2 & 0 \\ -6 & 0 & 5 \end{pmatrix}$
- c.  $A + B$  and  $B + A$  both exist and  $A + B = B + A$
- d.  $A + C$  and  $C + A$  both exist and  $A + C = C + A$
- e. None of the others

## Question 12

Let  $A = \begin{pmatrix} 1 & -1 \\ -3 & 2 \end{pmatrix}$ ,  $B = \begin{pmatrix} -4 & -1 \\ 0 & -3 \end{pmatrix}$  and  $C = \begin{pmatrix} 1 & -1 & 0 \\ -3 & -2 & 5 \end{pmatrix}$ .

- a.  $A \times B$  exists and its value is  $A \times B = \begin{pmatrix} -4 & 2 \\ 12 & -3 \end{pmatrix}$
- b.  $A \times C$  exists
- c.  $A \times B$  and  $B \times A$  both exist and  $A \times B = B \times A$
- d.  $A \times C$  and  $C \times A$  both exist and  $A \times C = C \times A$
- e. None of the others

## Question 13

Consider a matrix  $A \in \mathcal{M}_3(\mathbb{R})$  and let  $I_3$  denote the identity matrix in  $\mathcal{M}_3(\mathbb{R})$ . Then:

- a.  $I_3 = \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$
- b.  $A \times I_3 = I_3$
- c.  $A \times I_3 = A$
- d. None of the others

### Question 14

Let  $(A, B, C) \in (\mathcal{M}_3(\mathbb{R}))^3$ . Which of these properties is(are) true:

- a.  $(AB)C = A(BC)$
- b.  $(A + B)^2 = A^2 + B^2$
- c.  $A \times (2C) = 2(A \times C)$
- d.  $A \times B = 0 \implies A = 0$  or  $B = 0$ , where 0 denotes the zero matrix of  $\mathcal{M}_3(\mathbb{R})$ .
- e. None of the others

### Question 15

Let  $f$  be an endomorphism of  $\mathbb{R}^3$  whose matrix in the standard basis of  $\mathbb{R}^3$  as input and output basis is

$$A = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$$

Then we know that:

- a.  $f((0, 1, 0)) = (4, 5, 6)$
- b.  $f((0, 1, 0)) = (2, 5, 8)$
- c. We cannot know the value of  $f((0, 1, 0))$

### Question 16

Consider the linear map  $f : \begin{cases} \mathbb{R}^3 & \longrightarrow \mathbb{R}^2 \\ (x, y, z) & \mapsto (x + 2z, -4y - z) \end{cases}$

The matrix of  $f$  in the standard basis  $\mathcal{B}$  of  $\mathbb{R}^3$  as input and the standard basis  $\mathcal{B}'$  of  $\mathbb{R}^2$  as output basis is:

- a.  $\text{Mat}_{\mathcal{B}, \mathcal{B}'}(f) = \begin{pmatrix} 1 & 0 \\ 0 & -4 \\ 2 & -1 \end{pmatrix}$
- b.  $\text{Mat}_{\mathcal{B}, \mathcal{B}'}(f) = \begin{pmatrix} 1 & 0 & 2 \\ 0 & -4 & -1 \end{pmatrix}$
- c. None of these matrices

### Question 17

Let  $A \in \mathcal{M}_3(\mathbb{R})$ . The sense of the property "A is invertible" is:

- a.  $\exists B \in \mathcal{M}_3(\mathbb{R})$  such that  $AB = BA = A$
- b.  $\exists B \in \mathcal{M}_3(\mathbb{R})$  such that  $AB = BA = I_3$  where  $I_3$  denotes the identity matrix of  $\mathcal{M}_3(\mathbb{R})$
- c.  $\exists B \in \mathcal{M}_3(\mathbb{R})$  such that  $A + B = B + A = I_3$  where  $I_3$  denotes the identity matrix of  $\mathcal{M}_3(\mathbb{R})$
- d. None of the others

### Question 18

The inverse matrix of  $A = \begin{pmatrix} 1 & 2 \\ 1 & 3 \end{pmatrix}$  is  $A^{-1} = \begin{pmatrix} 3 & -1 \\ -2 & 1 \end{pmatrix}$

- ✓ a. True  
b. False

### Question 19

Consider a matrix  $A = (a_{i,j}) \in \mathcal{M}_{n,p}(\mathbb{R})$  where  $n$  and  $p$  are two non-zero natural numbers. Then:

- a. The coefficient  $a_{1,2}$  is at the first row and second column of  $A$   
✓ b. The coefficient  $a_{1,2}$  is at the second row and first column of  $A$

### Question 20

Last question of the year :) There is no trap in the question!

Find the last coefficient of the matrix  $A$  below. Note the the coefficients satisfy logical connections:

$$A = \begin{pmatrix} 0 & 2 & 4 \\ 6 & 8 & 10 \\ 12 & 14 & ? \end{pmatrix}$$

- ✓ a. 16  
b. 18  
c. 20  
d. None of the others

## ADP MCQ B4

20/5/24

### Grammar

Fill in the blanks with the correct answer:

21. As soon as Betty \_\_\_\_ the ripe apples from her tree, she \_\_\_\_ them for an apple pie.

- A) will pick / uses
- B) will have picked / will have been using
- C) picks / is going to use
- D) will pick / will use

22. Mona \_\_\_\_ on the accounts all day by the time she \_\_\_\_ home.

- A) works / goes
- B) will work / is going to go
- C) will have been working / goes
- D) will have been working / will have been going

23. After Michel \_\_\_\_ the train to Los Angeles, he \_\_\_\_ writing his report on his laptop.

- A) catches / is going to finish
- B) is going to catch / is going to finish
- C) will have caught / will finish
- D) catches / finishes

24. Robert \_\_\_\_ into his own apartment when he \_\_\_\_ a job.

- A) will have moved / will find
- B) is going to move / finds
- C) moves / will find
- D) will move / will find

25. I \_\_\_\_ all my files before I \_\_\_\_ my computer.

- A) will have saved / will shut down
- B) will be saving / will shut down
- C) will have been saving / shut down
- D) will save / shut down



26. He's never going to stop talking. In 15 more minutes, we \_\_\_\_\_ to him lecture for three solid hours.

- ✓ A) will have been listening
- B) will listen
- C) will be listening
- D) will have listened

27. Can you believe it? According to our grammar teacher, by the end of this semester, she \_\_\_\_\_ more than 3,000 students from 42 different countries!

- A) will teach
- B) will be teaching
- C) will have been teaching
- ✓ D) will have taught

28. This is the longest flight I have ever taken. By the time we get to New Zealand, we \_\_\_\_\_ for 13 hours. I'm going to be exhausted.

- ✓ A) will have been flying
- B) will have flown
- C) will fly
- D) will be flying

29. By 10:00 yesterday, she had called three new clients. Tomorrow, by 10:00, she \_\_\_\_\_ three new clients.

- A) will call
- B) will have called
- C) will be calling
- D) is going to call

30. She went to lunch at noon and had a sandwich and a bowl of soup. Tomorrow she \_\_\_\_\_ at noon and \_\_\_\_\_ a sandwich and a bowl of soup.

- A) will be going / will be having
- B) will go / will have
- C) will have gone / will have
- D) will go / will have had