# Algorithmics Correction Midterm Exam #1

Undergraduate  $1^{st}$  year S1 - Epita

#### Solution 1 (Abstract Types: Recursive lists – 5 points)

1.

The operation search is defined only when the searched element exists. Therefore, it is a precondition. Then we have the three axioms applying the observer ispresent to the internal operations emptylist and cons. In order: the element e does not exist in an empty list, the element e exists in a list in which it is equal to the first element and otherwise... try again (it may exist in the tail of the list). Then the axiom explaining that the box returned by search(e, $\lambda$ ) is the one which contains e.

#### PRECONDITIONS

```
search(e, \lambda) is-defined-iaoi ispresent(e, \lambda) = true
AXIOMS
ispresent \ (e, emptylist) = false
e = e' \Rightarrow ispresent \ (e, cons(e', \lambda)) = true
e \neq e' \Rightarrow ispresent \ (e, cons(e', \lambda)) = ispresent \ (e, \lambda)
contents(search(e, \lambda)) = e
```

2.

Two axioms suffice. The first says that the concatenation result of an empty list and a list  $\lambda$  is the list  $\lambda$ , which means that the elements of the second list are retained in order and number. The second axiom explains that we also keep in order and number the elements of the first list. How? Showing that if the concatenation is done before or after building (cons) the list, the result is the same, which means that the concatenation modifies neither the order nor the elements.

#### AXIOMS

```
concatenate (emptylist, \lambda 2) = \lambda 2
concatenate (cons(e, \lambda), \lambda 2) = cons(e, concatenate (\lambda, \lambda 2))
```

### Solution 2 (Deletion) - 4 points

# Specifications:

Write the function delete x list that removes the first appearance of the value x (if it is present) from the sorted (in increasing order) list list.

```
# let rec delete x = function
        [] -> []
        | h::q when h > x -> h :: q
        | h::q when h = x -> q
        | h::q -> h::delete x q ;;
val delete : 'a -> 'a list -> 'a list = <fun>
# delete 4 [1; 2; 2; 3; 4; 4; 4; 5];
- : int list = [1; 2; 2; 3; 4; 4; 5]
```

#### Solution 3 (Insertion at the rank i-5 points)

**Spécifications:** Write the function  $insert_nth \ x \ i \ list$  that inserts the value x at the rank i in the list list.

The function has to raise an exception  $Invalid\_argument$  if i is negative or zero, an exception Failure if the list is too short.

# Solution 4 (Search) - 4 points

#### **Specifications:**

Write the function search\_both  $list\ a\ b$  that tests whether the two distinct values a and b are in the list list.

```
# let search v1 v2 l =
     let rec aux1 v l = match l with
         [] -> false
        |e::1 -> v = e || aux1 v 1
     in
     let rec aux2 1 = match 1 with
         [] -> false
        |e::l \rightarrow if e = v1 then
                      aux1 v2 l
                  if e = v2 then
                      aux1 v1 l
                  else
                      aux2 1
     in aux2 1
 ;;
  val search : 'a -> 'a list -> bool = <fun>
Another version:
 # let search v1 v2 l =
     let rec aux 1 found1 found2 = match 1 with
         [] -> false
        |e::l \rightarrow if e = v1 then
                      found2 || aux 1 true false
                  else
                  if e = v2 then
                      found1 || aux l false true
```

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#### Solution 5 (Mystery – 2 points)

#### 1. Specifications:

Give the results of the successive evaluations of the following phrases.

```
# let go = function
        [] -> []
      | e::list ->
        let rec what x = function
            [] -> []
          | e::list -> (e * x)::(what e list)
        in
        what e list;;
 val go : int list -> int list = <fun>
# go [1; 1; 1; 1; 1] ;;
 - : int list = [1; 1; 1; 1]
# go [42] ;;
 - : int list = []
# go [1; 2; 3; 4; 5] ;;
 - : int list = [2; 6; 12; 20]
# go [2; 21; 2; 21; 2; 21] ;;
 - : int list = [42; 42; 42; 42; 42]
```